



**De Cifris incontra Milano**

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# **Blockchains, and the search for Cryptographic Boolean Functions**

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- Associate Professor at the Department of Informatics, Systems and Communication (DISCo) of the University of Milan – Bicocca
- Founder and current director of Bicocca Security Lab
  - interests also in Cybersecurity
  - inside the lab, Luca Mariot and me have competencies on Cryptography
- Teacher of a course on Information Theory and Cryptography for the Master Degree on Computer Science, since 2008
- Supervisor of many bachelor (90+) and master (30+) theses
- Supervisor of two Ph.D. theses on Cryptography
- Supervisor of a post-doc research project on Cryptography
- Member of CINI Cybersecurity Lab (Milan – Bicocca node)

- BiS Lab = Bicocca **Security** Lab
- **Interdepartmental** lab: Computer Science + Law
- The founders (from left to right):
  - > Prof. **Alberto Leporati**  
(Computer Science)
  - > Prof. **Andrea Rossetti**  
(Law)
  - > Prof. **Claudio Ferretti**  
(Computer Science)

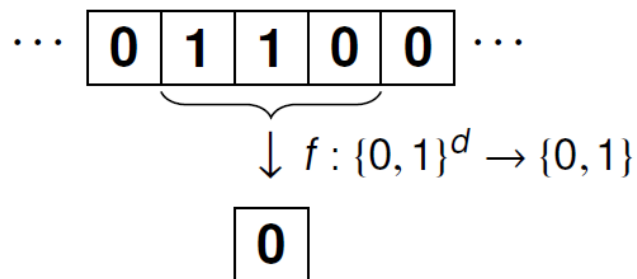




- Law assistance + security audits for private companies
  - Compliance with the new regulation and laws about data privacy (GDPR)
- Courses and dissemination of cybersecurity ideas and principles
  - Training courses for students
  - Participation to public events:
    - ❖ “MEETmeTONIGHT: Face to face with research”
    - ❖ Digital Week
    - ❖ Bookcity
- Participation to EU and Regional research calls

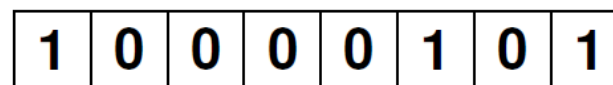
- Theoretical foundations of cryptographic primitives
- Search for Boolean functions with good cryptographic properties:  
*k*-resiliency, nonlinearity, balancedness
- Relations with Secret Sharing Schemes, Orthogonal Arrays, combinatorial designs, linear codes
- Relations with parallel models of computation, mainly Boolean circuits and Cellular Automata

● CA-based **block cipher design**:

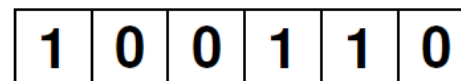



- **local rules** are Boolean functions
- strong functions can be used for **stream ciphers** and for **PRNGs**

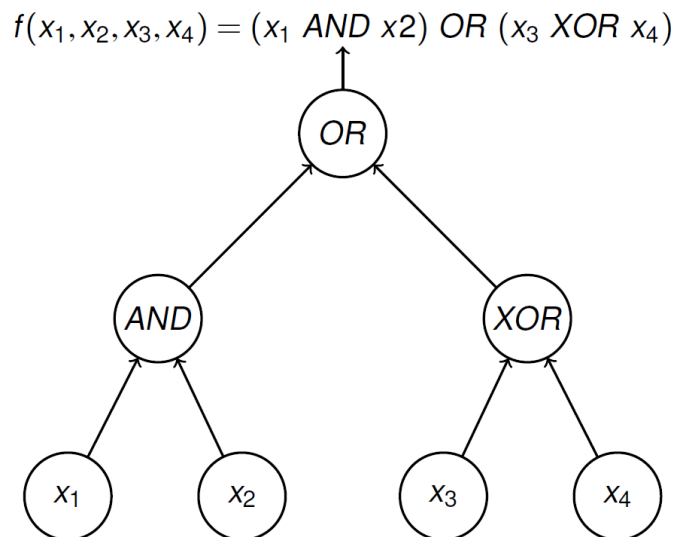
- **global rules** can be seen as **S-boxes**
- **goal**: find S-boxes with **high nonlinearity** and with **low differential uniformity**



$\Downarrow F : \{0, 1\}^n \rightarrow \{0, 1\}^m$



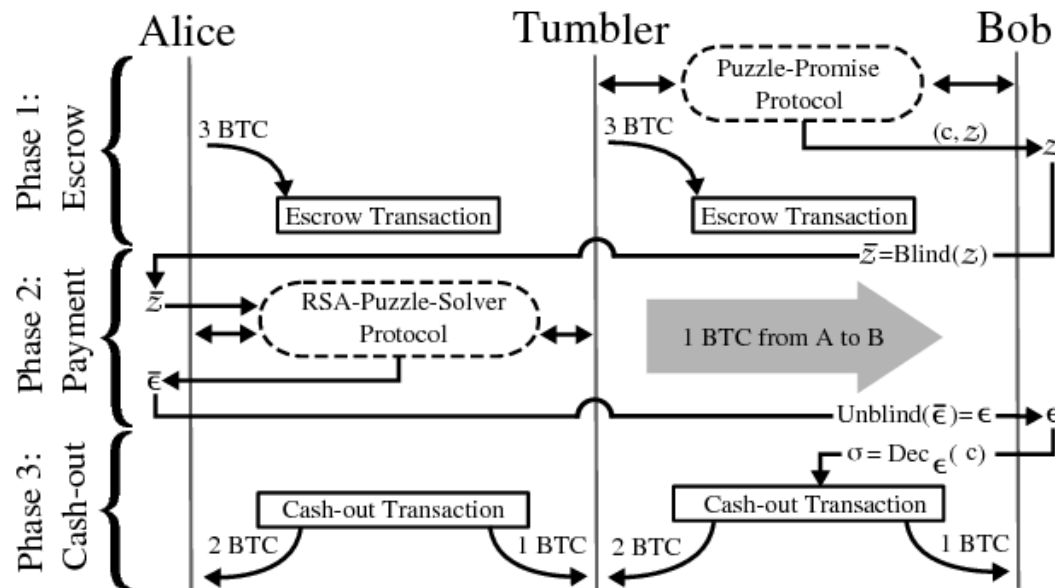
- The **number of Boolean functions** grows in a **double exponential way** wrt to the number  $n$  of inputs:  $2^{2^n}$ . Exhaustive search becomes impossible
- **Evolutionary techniques** used: PSO, Genetic Algorithms, Genetic Programming
- Search spaces:
  - truth tables of Boolean functions
  - Walsh spectra of pseudo-Boolean real functions
  - trees of Boolean operators
- Example of encoding in GP: 





- Results obtained:
  - for  $n = 4$  and  $n = 5$ , we obtained CA rules inducing S-boxes with **optimal crypto properties**, and with implementation cost similar to or slightly better than the state of the art in the literature
  - for  $n > 5$ , GP finds S-boxes with **optimal cryptographic properties** up to  $n = 7$ , but with **too high implementation costs**
- In general, Genetic Programming seems to work better than Genetic Algorithms (**Why?**)

● Modification of the TumbleBit payment protocol:



- in the context of **permissioned** blockchains
- in order to obtain **transferability of tokens** between receivers
- without making the two receivers linkable

- Design of blockchain-based applications
  - supply chain management
  - definition of utility (crypto) tokens backed by tangible assets
  - development of smart contracts with Ethereum (Solidity) and Hyperledger (Go Lang)



ethereum  
BLOCKCHAIN APP PLATFORM



Solidity



**HYPERLEDGER**



Two use cases:

- **Anti-counterfeiting** of luxury **clothes** and **accessories**, using a blockchain + RFIDs
  - each cloth / accessory has a unique RFID
  - every production / assembly / transportation / sell operation is written on the blockchain
  - it becomes incredibly difficult to sell counterfeit items!
- **Storage of sensor data** from (non-autonomous) vehicles
  - hashes of contents of the car's black box are regularly saved on the blockchain
  - when needed, the driver can prove that his/her data have not been altered



Thanks for your attention!



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